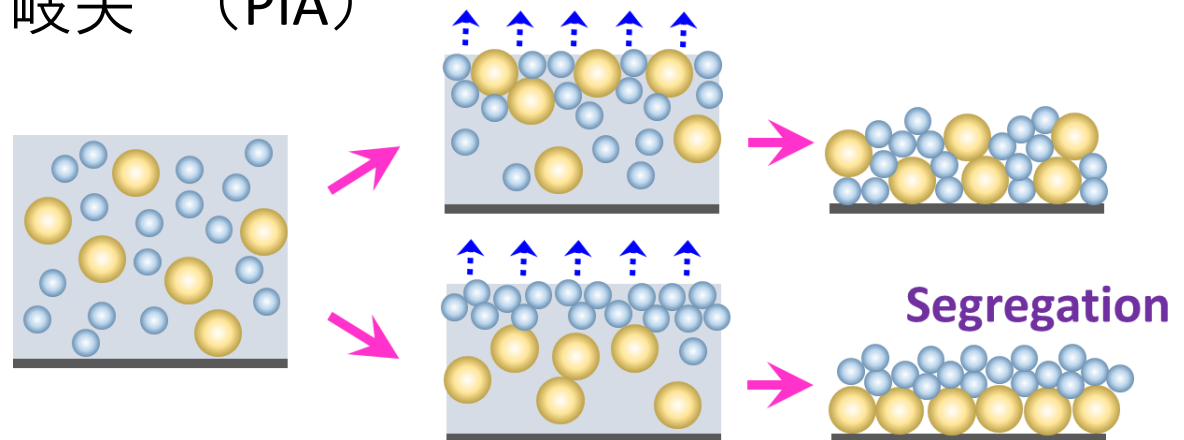
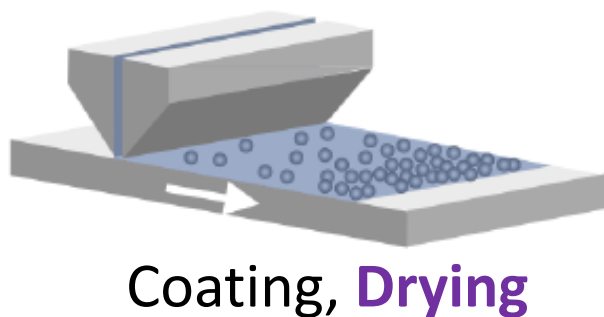


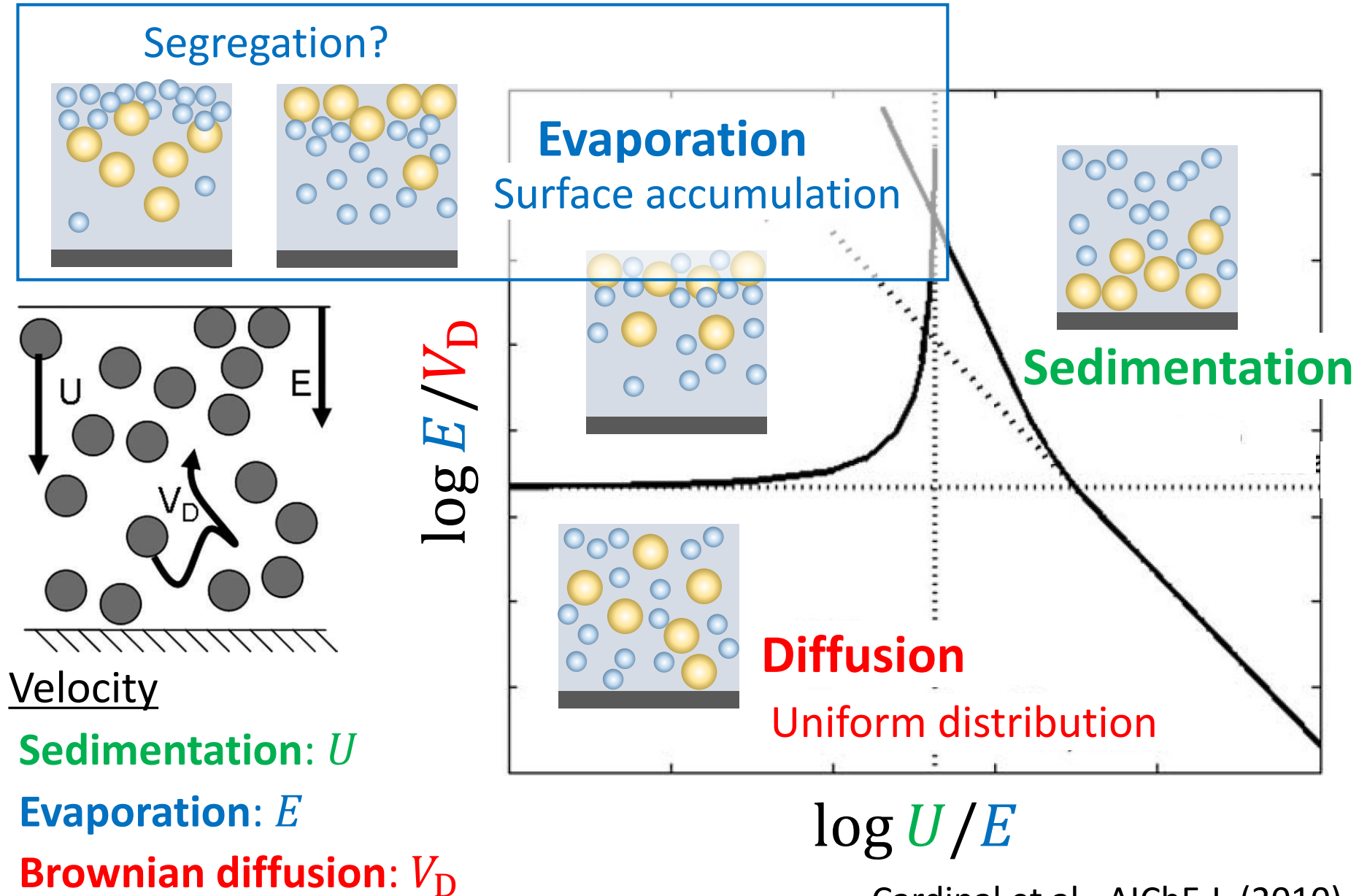
# 二峰性微粒子分散液の乾燥における 偏析現象のメカニズム

## Mechanism of Segregation in Drying Bimodal Colloidal Suspensions

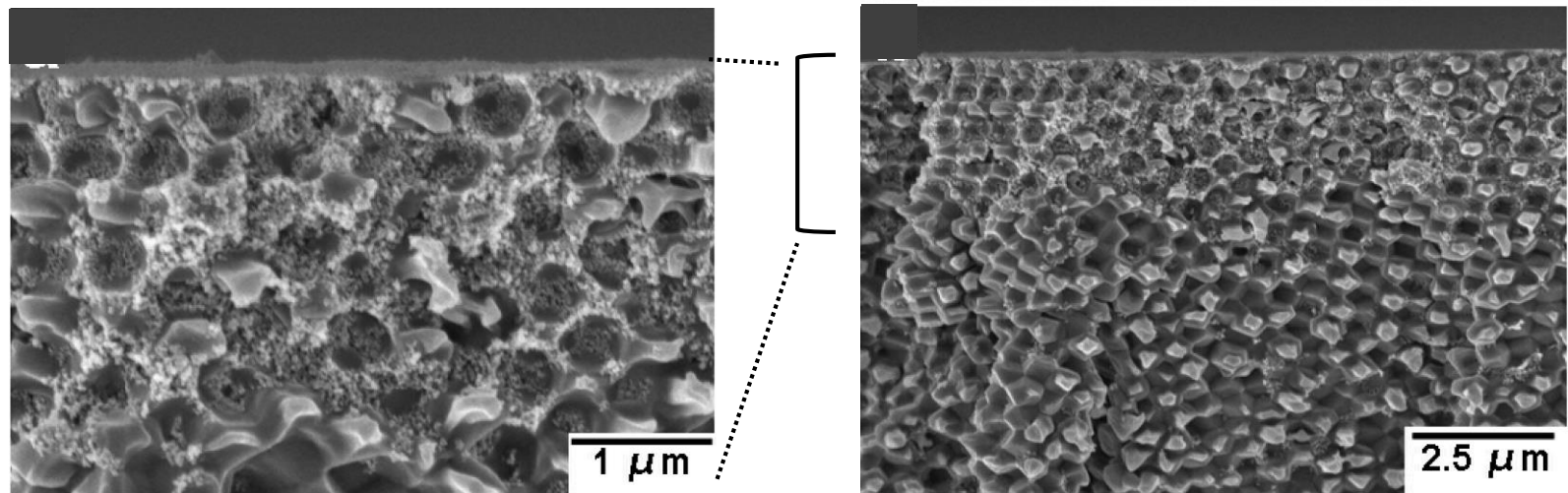
- 辰巳 怜 (東大環安セ)
- 岩男拓哉 (東大院工)
- 小池 修 (PIA)
- 辻 佳子 (東大環安セ/東大院工)
- 山口由岐夫 (PIA)



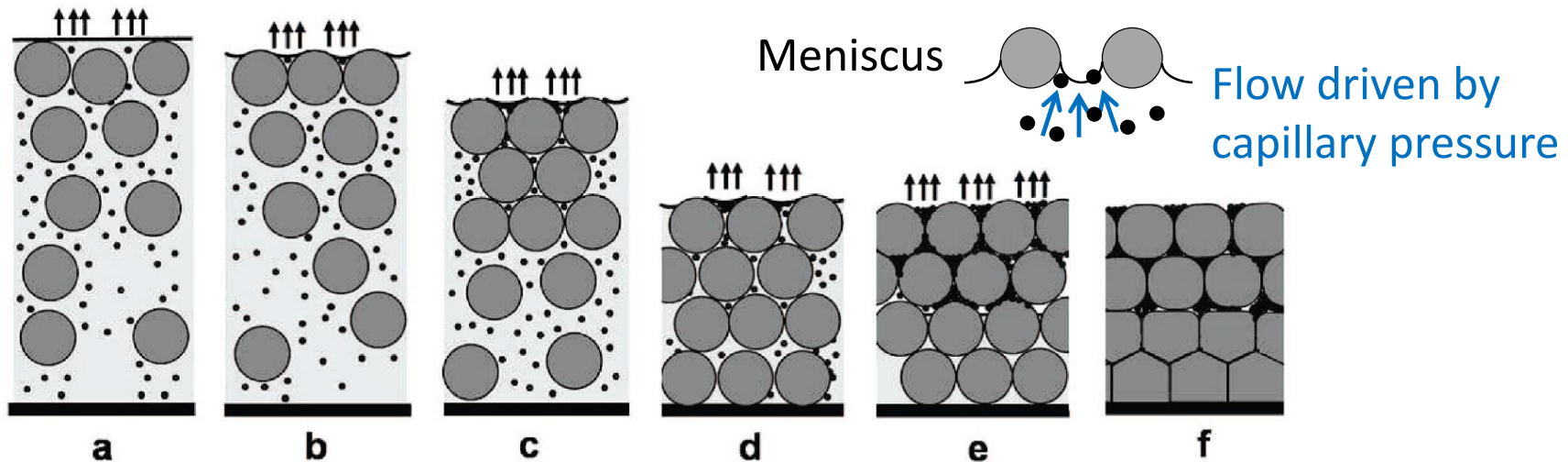
# Particle Distribution during Drying



# A Proposed Mechanism

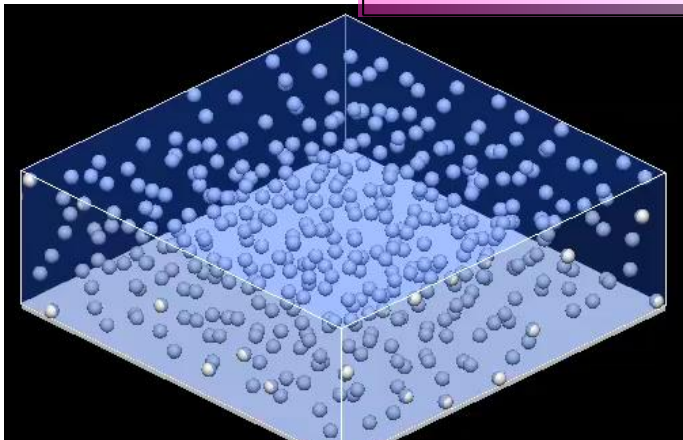
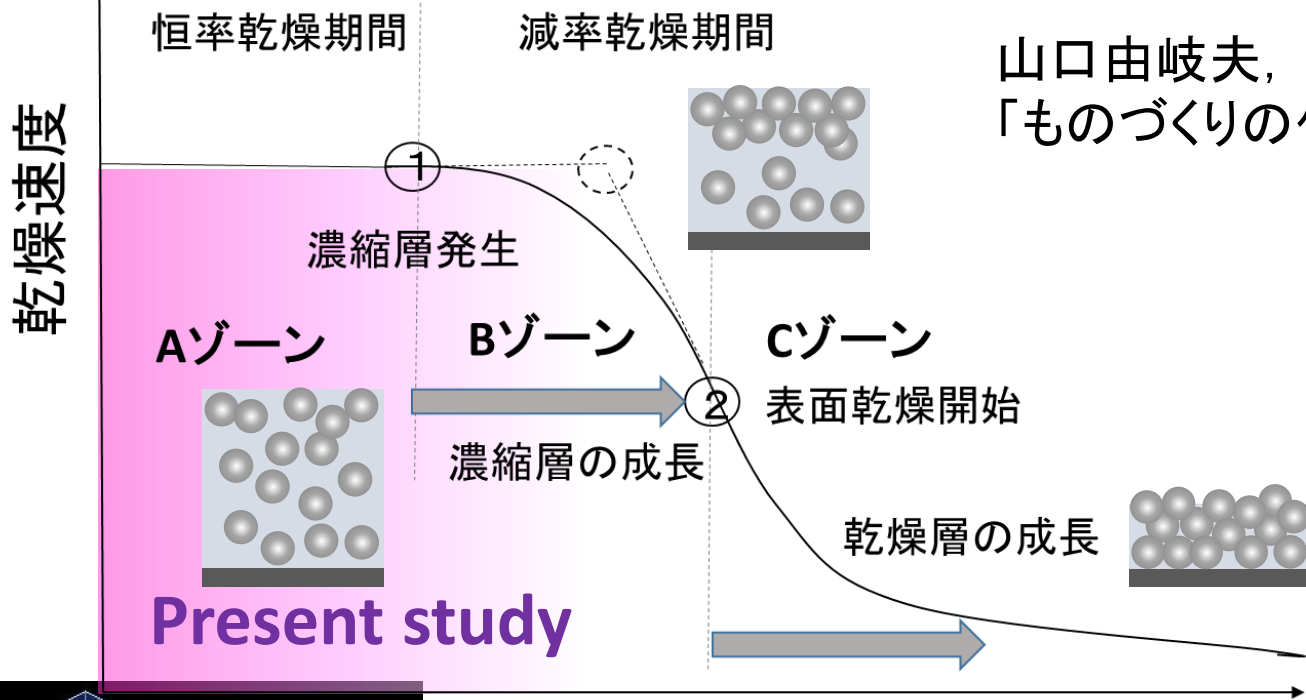


SEM images of the cross section of a dried silica (20 nm) / latex (550 nm) coating

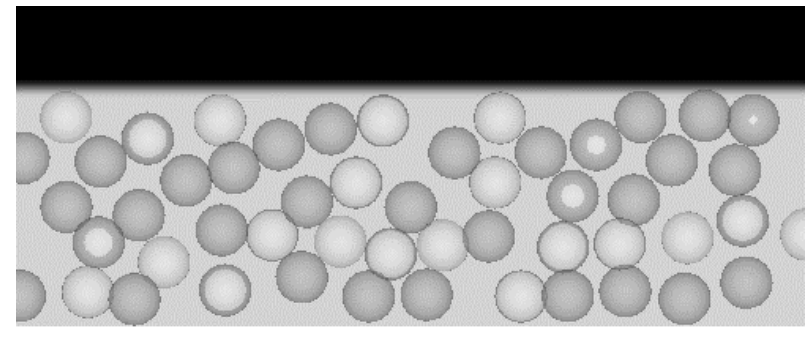


# Drying Curve of Colloidal Suspensions

山口由岐夫,  
「ものづくりの化学工学」



乾燥時間



# Objective

- ◆ Elucidation of the mechanism of segregation
- ◆ Analysis using a simple model
  - Brownian motion of particles
  - Free surface moving at constant rate
  - No consideration of gravity and fluid flow

# Langevin Equation

**Velocity**  $M_i \dot{V}_i = -\xi V_i + F_i^R + F_i^{\text{contact}} + F_i^{\text{capillary}}$

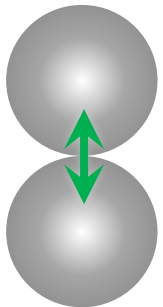
**Position**  $\dot{R}_i = V_i$

**Random force:** Stochastic variables obeying the Gaussian distribution

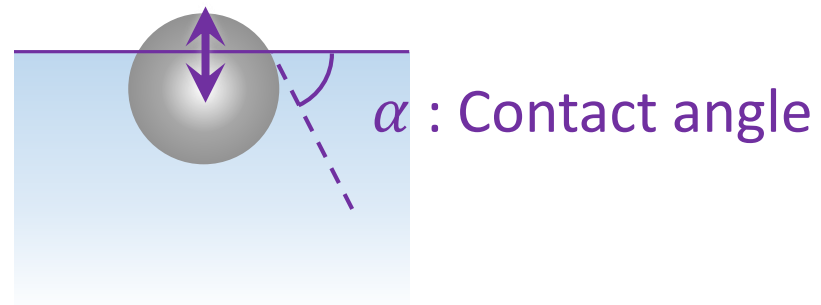
$$\langle F_{i\alpha}^R(t) \rangle = 0$$

$$\langle F_{i\alpha}^R(0) F_{i\beta}^R(t) \rangle = 2\xi k_B T \delta_{\alpha\beta} \delta(t) \quad \xi = 3\pi\eta d$$

**Contact force**



**Vertical capillary force**

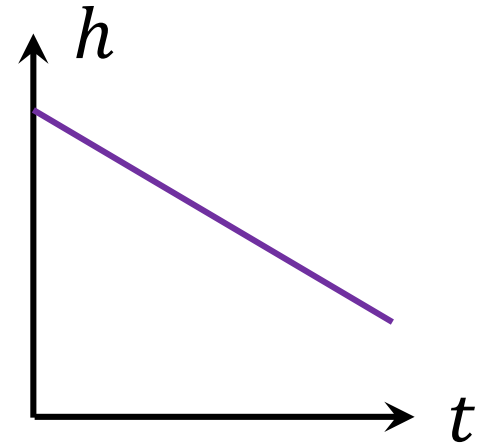


**Gravity and fluid flow** are not considered.

# Particle Drying Péclet Number

Film height  $h(t) = h_0 - v_e t$

- Constant evaporation rate  $v_e$

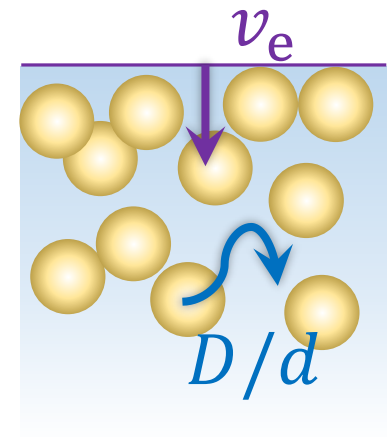


- Diffusion coefficient (Stokes-Einstein relation)


$$D = \frac{k_B T}{3\pi\eta d}$$

Particle drying Péclet number

$$\text{Pe} = \frac{(\text{Evaporation rate})}{(\text{Diffusion rate})} = \frac{v_e}{D/d} = \frac{v_e d}{D}$$



# Simulation Conditions

- Particle diameter **L:  $d$  S:  $\kappa^{-1}d$**
- Initial volume fraction  $h_0 = 50d$   
**L: 0.05 S: 0.05 (Total : 0.1)**
- Contact angle  $\alpha = 0$  

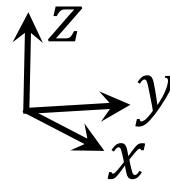
- Diameter ratio (L/S)  $\kappa = 1.5, 2, 4$



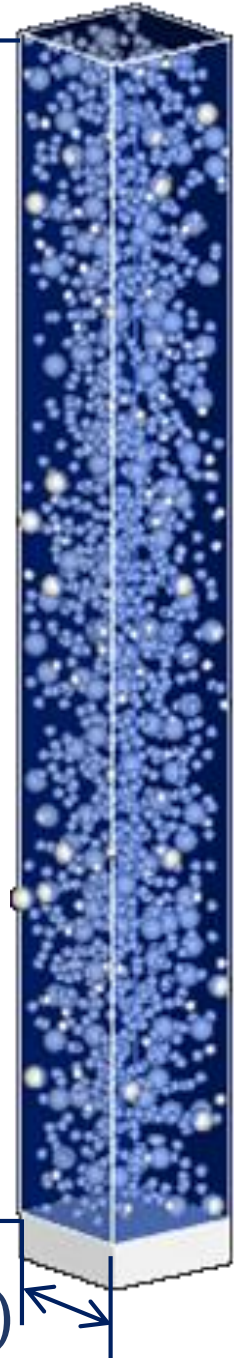
- Particle drying Péclet number (L)

$$Pe = 0.3 \sim 1000$$

Periodic boundaries:  $x, y$

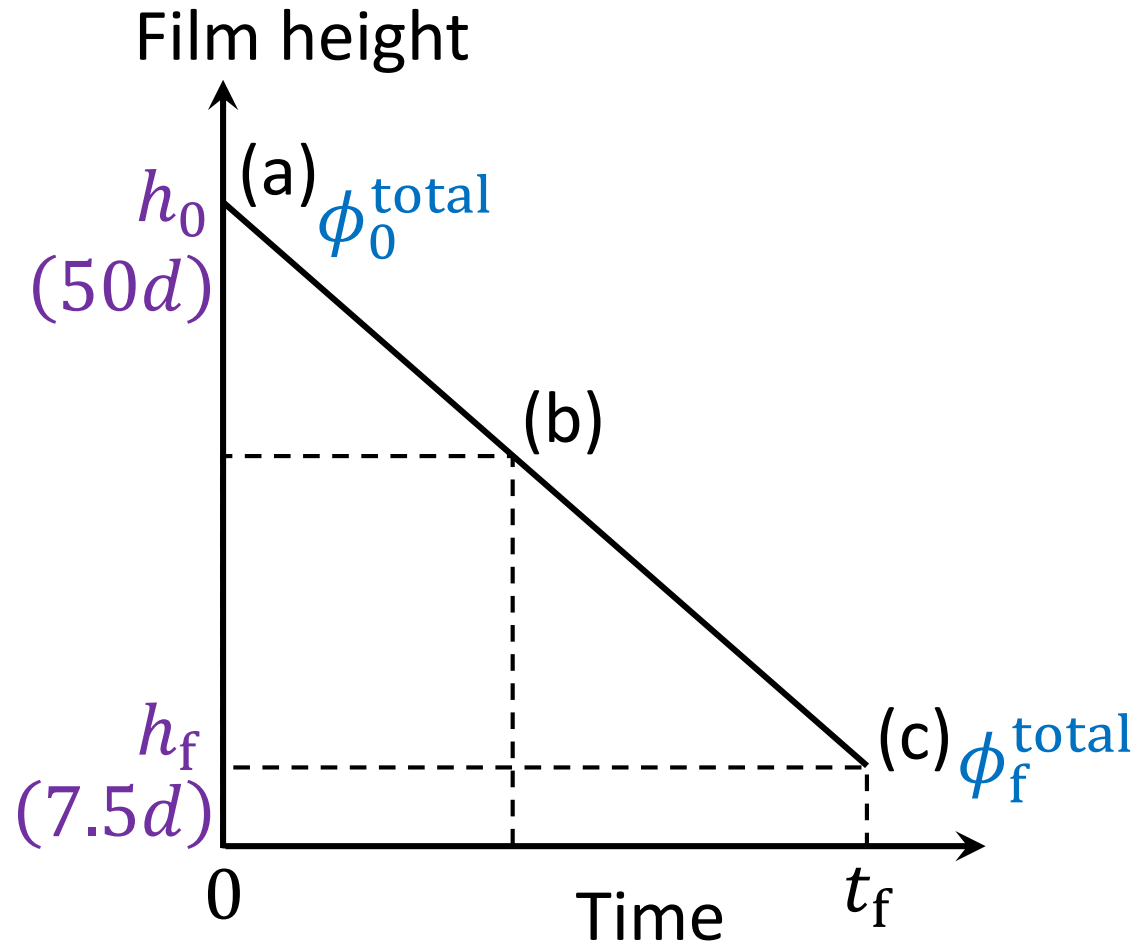
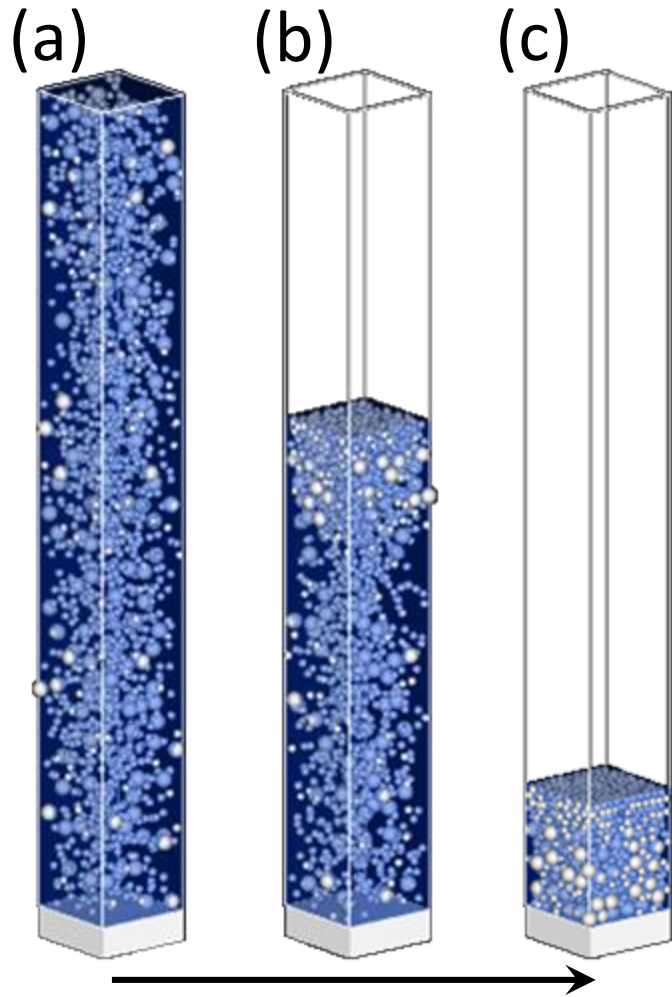


$6d$  ( $3d$ )





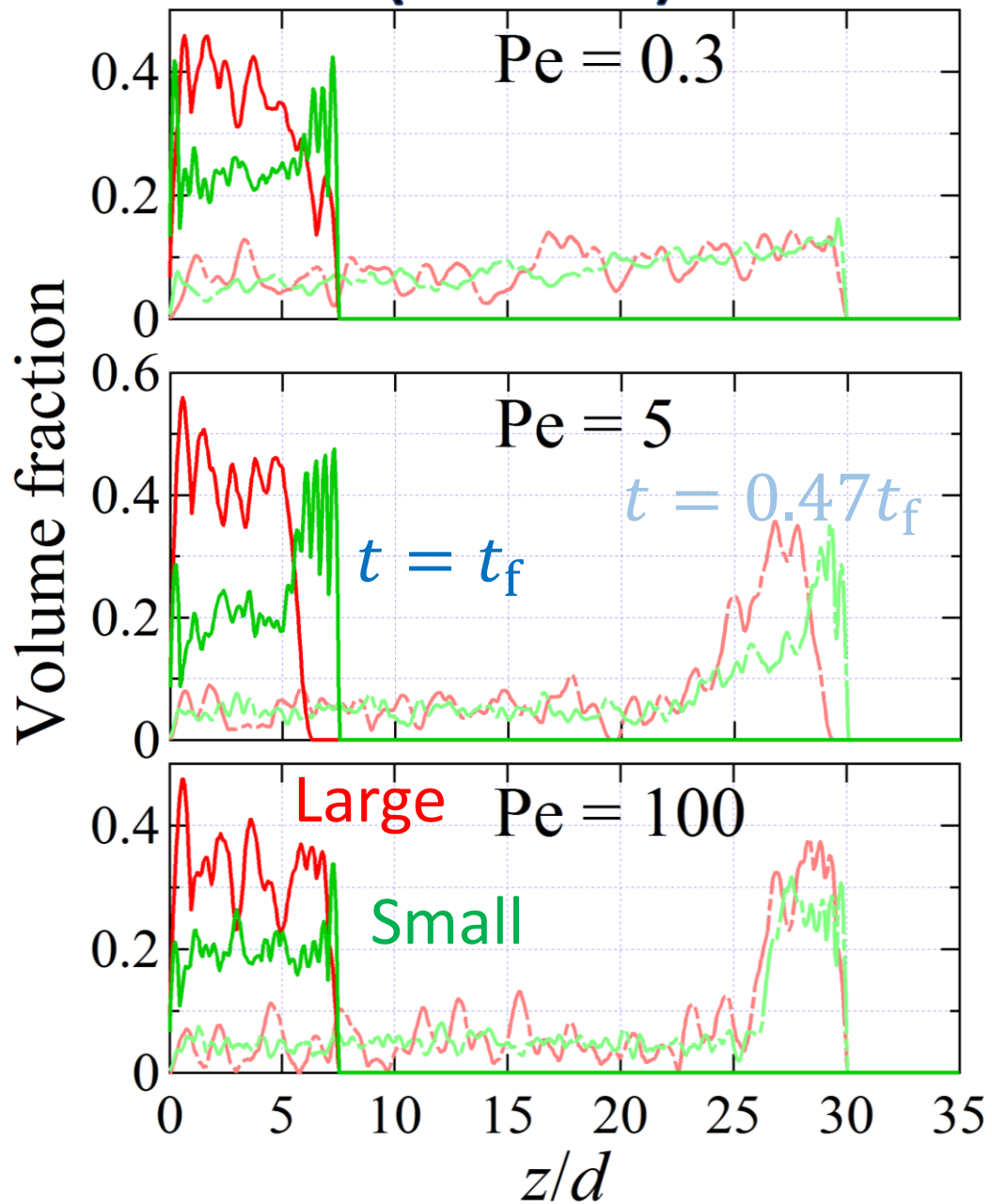
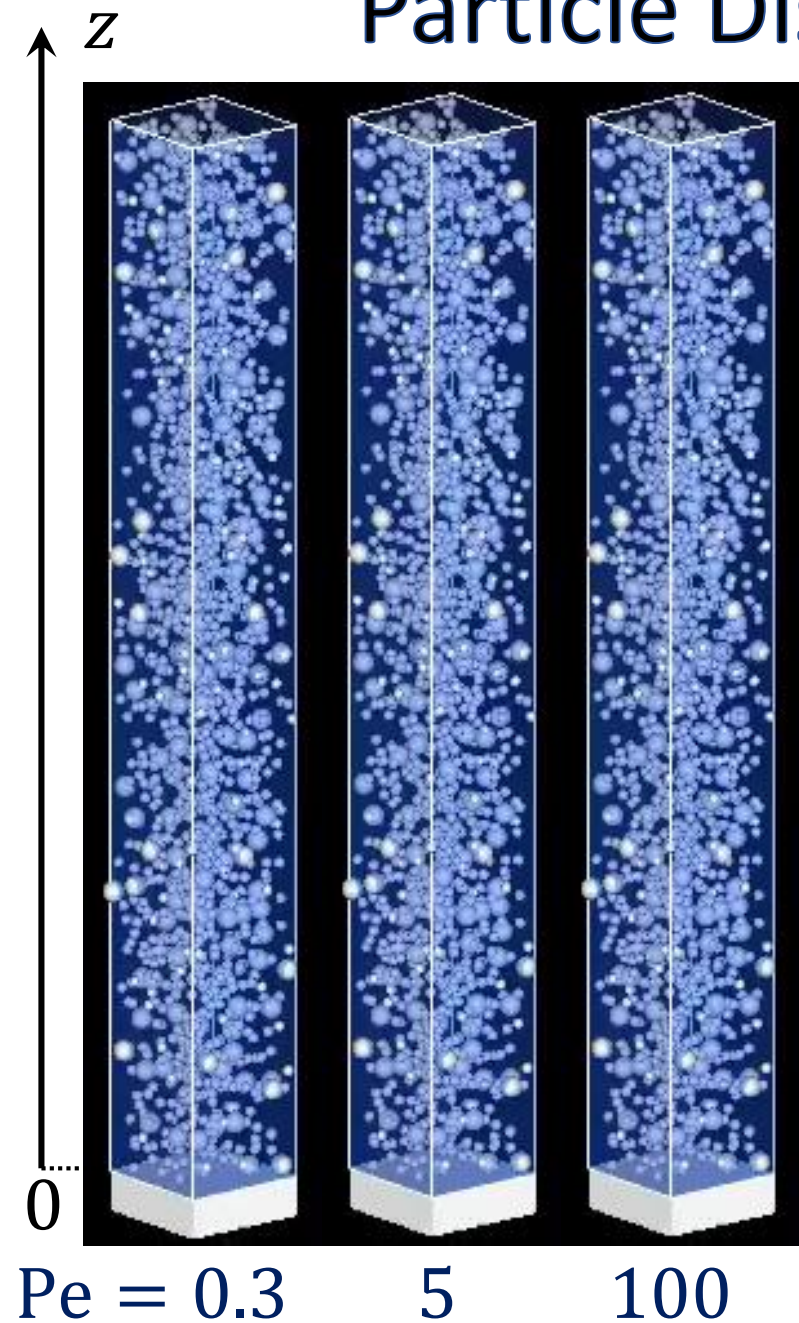
# Simulation Conditions



**Final state**

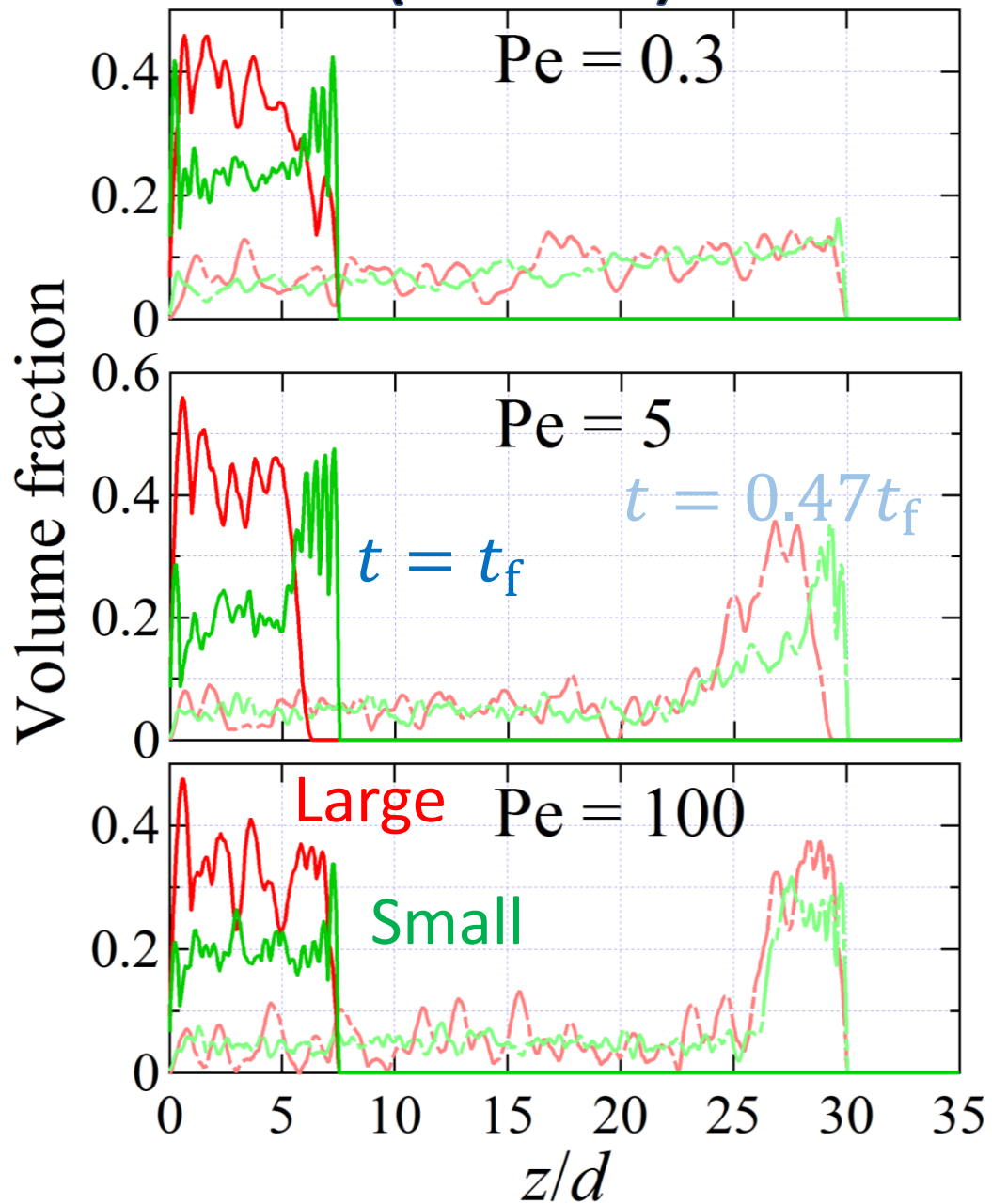
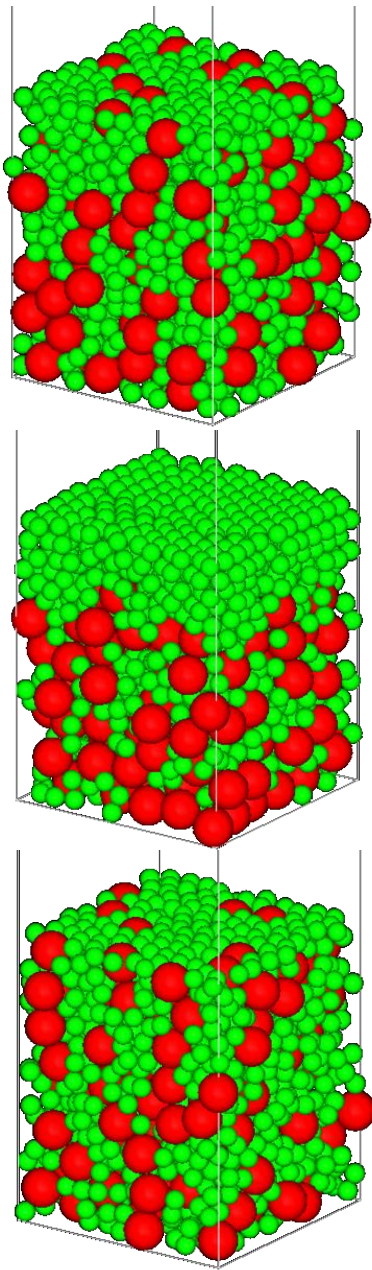
$$h_f = \frac{3}{20} h_0 = 7.5d \quad \phi_f^{\text{total}} = \frac{20}{3} \phi_0^{\text{total}} \approx 0.67$$

# Particle Distribution ( $\kappa = 2$ )



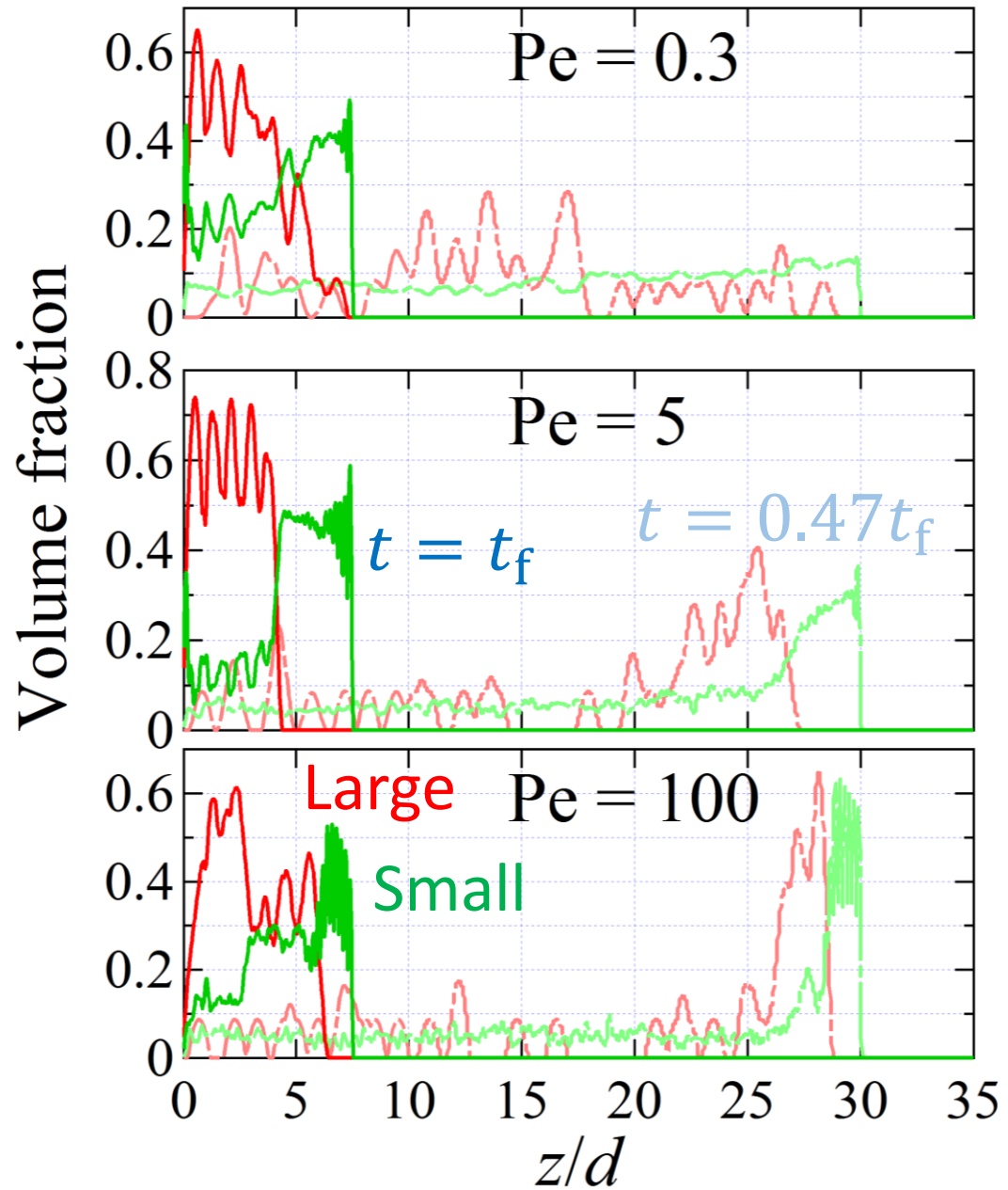
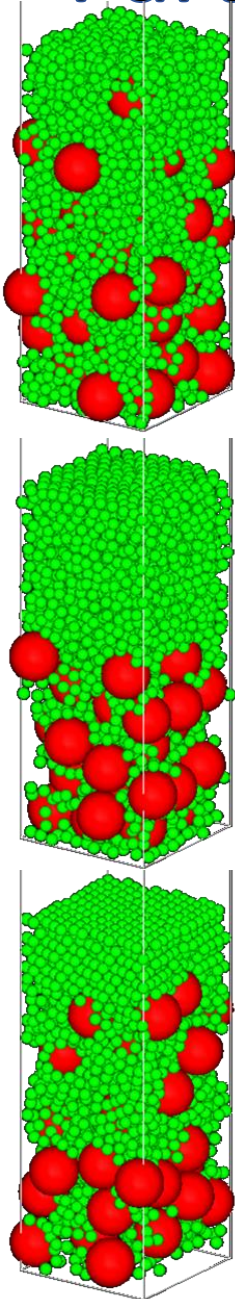
# Particle Distribution ( $\kappa = 2$ )

$t = t_f$



# Particle Distribution ( $\kappa = 4$ )

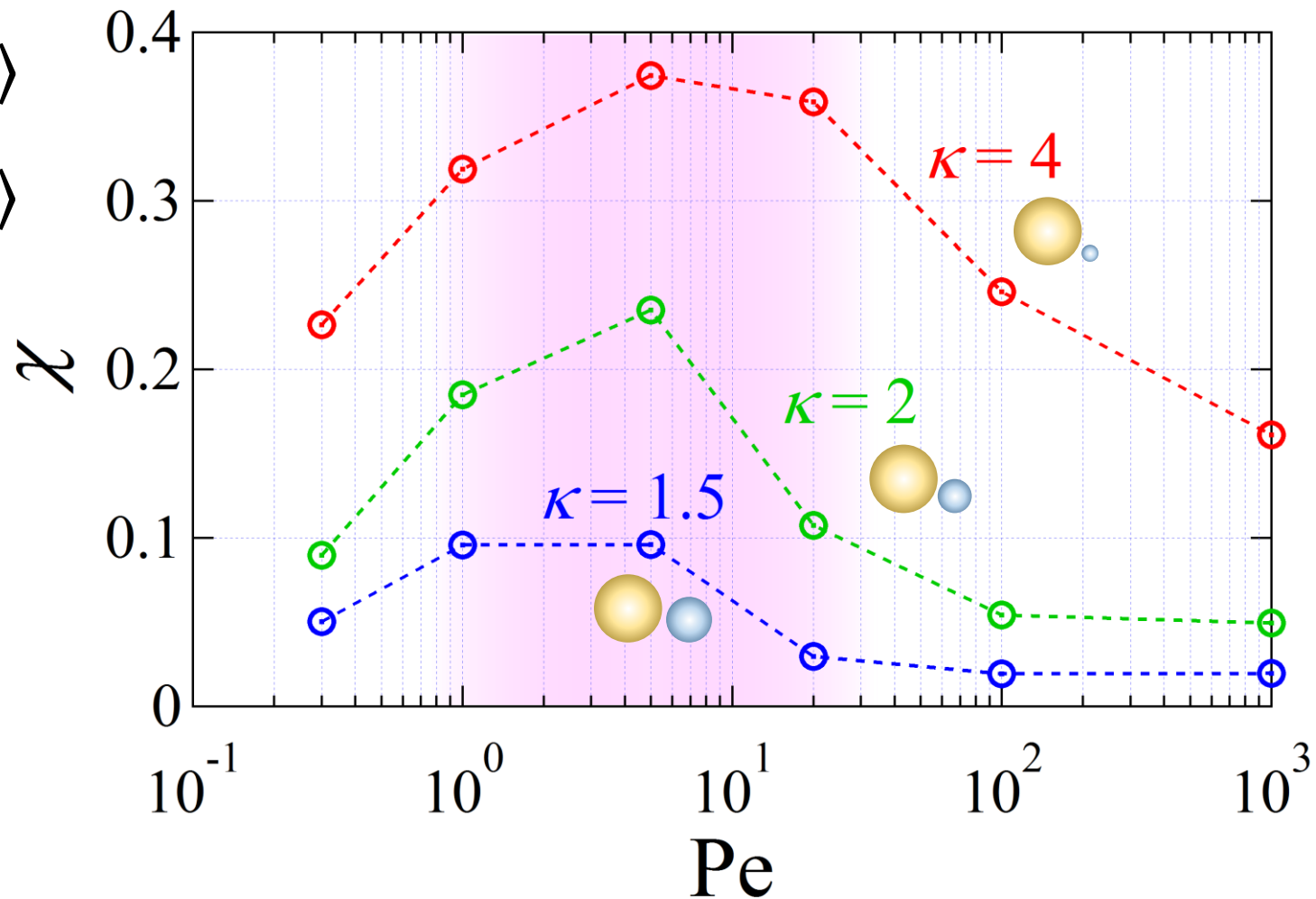
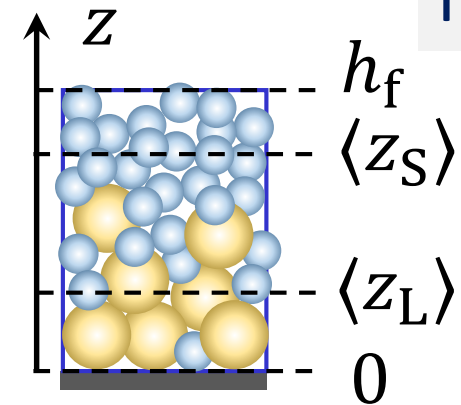
$t = t_f$



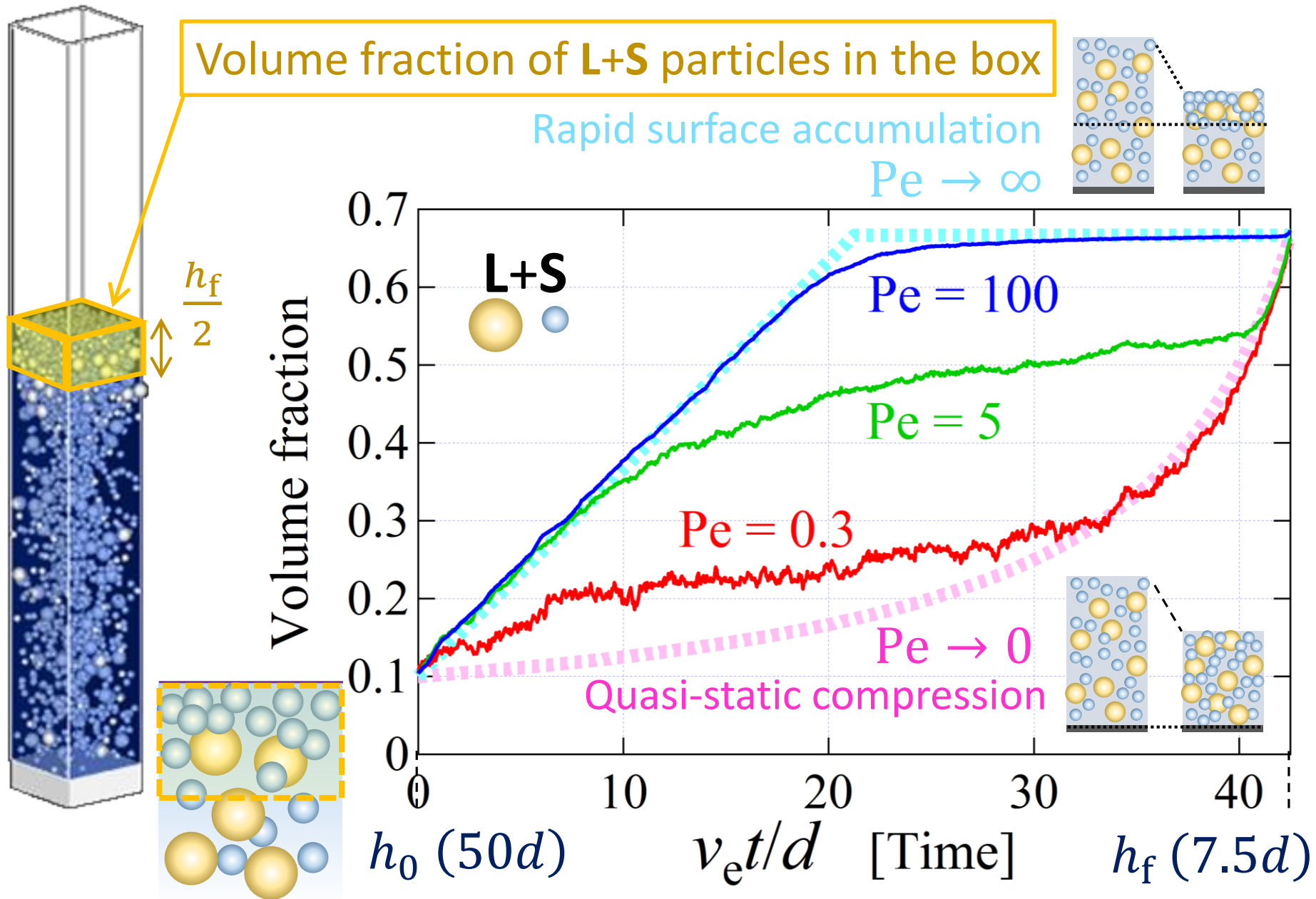
# Segregation in Final State

Average z-coordinate of the particles **L**:  $\langle z_L \rangle$  **S**:  $\langle z_S \rangle$

Indicator of segregation:  $\chi \equiv (\langle z_S \rangle - \langle z_L \rangle) / h_f$

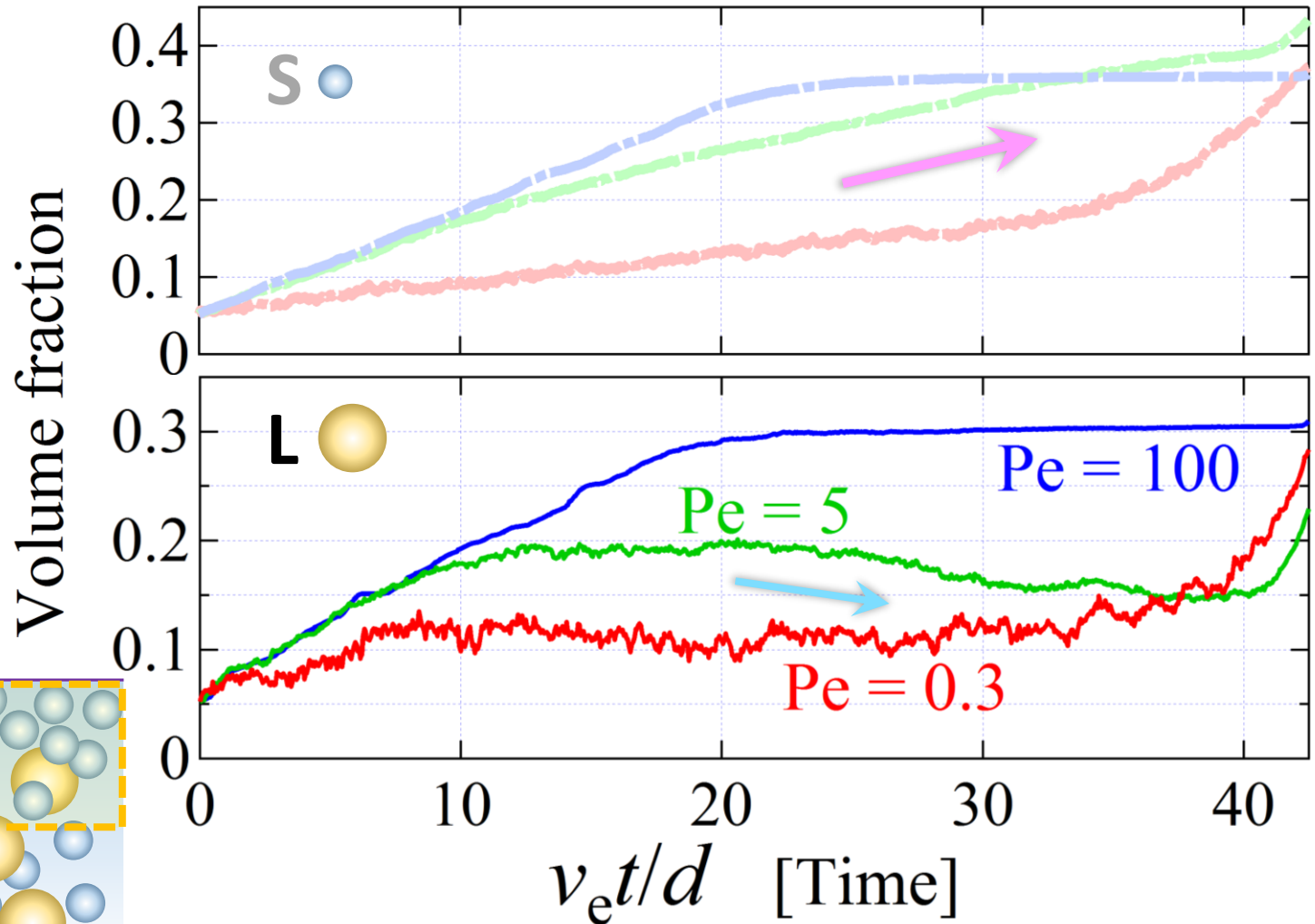
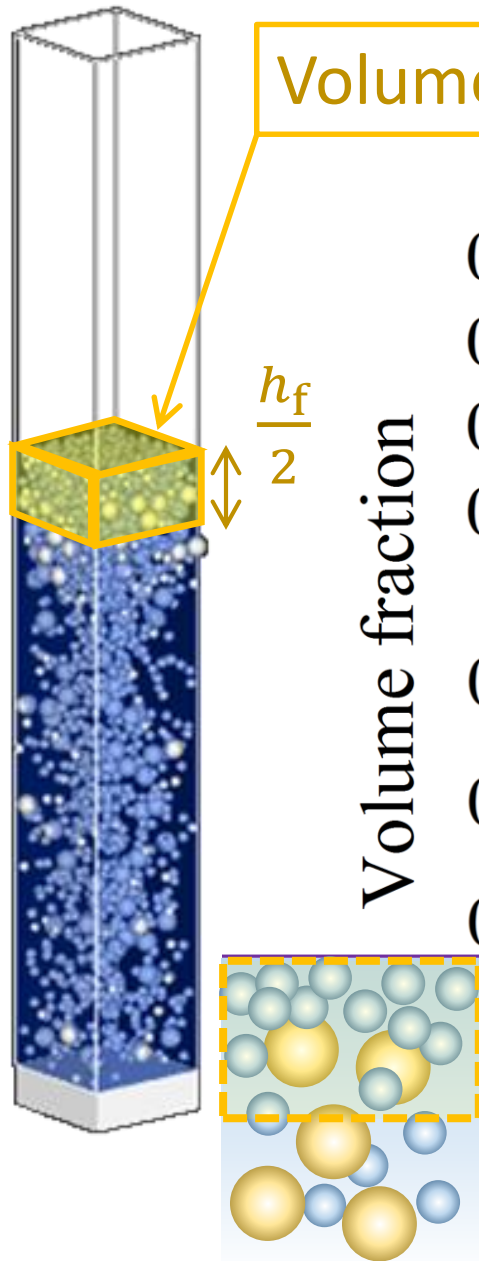


# Surface Accumulation ( $\kappa = 2$ )



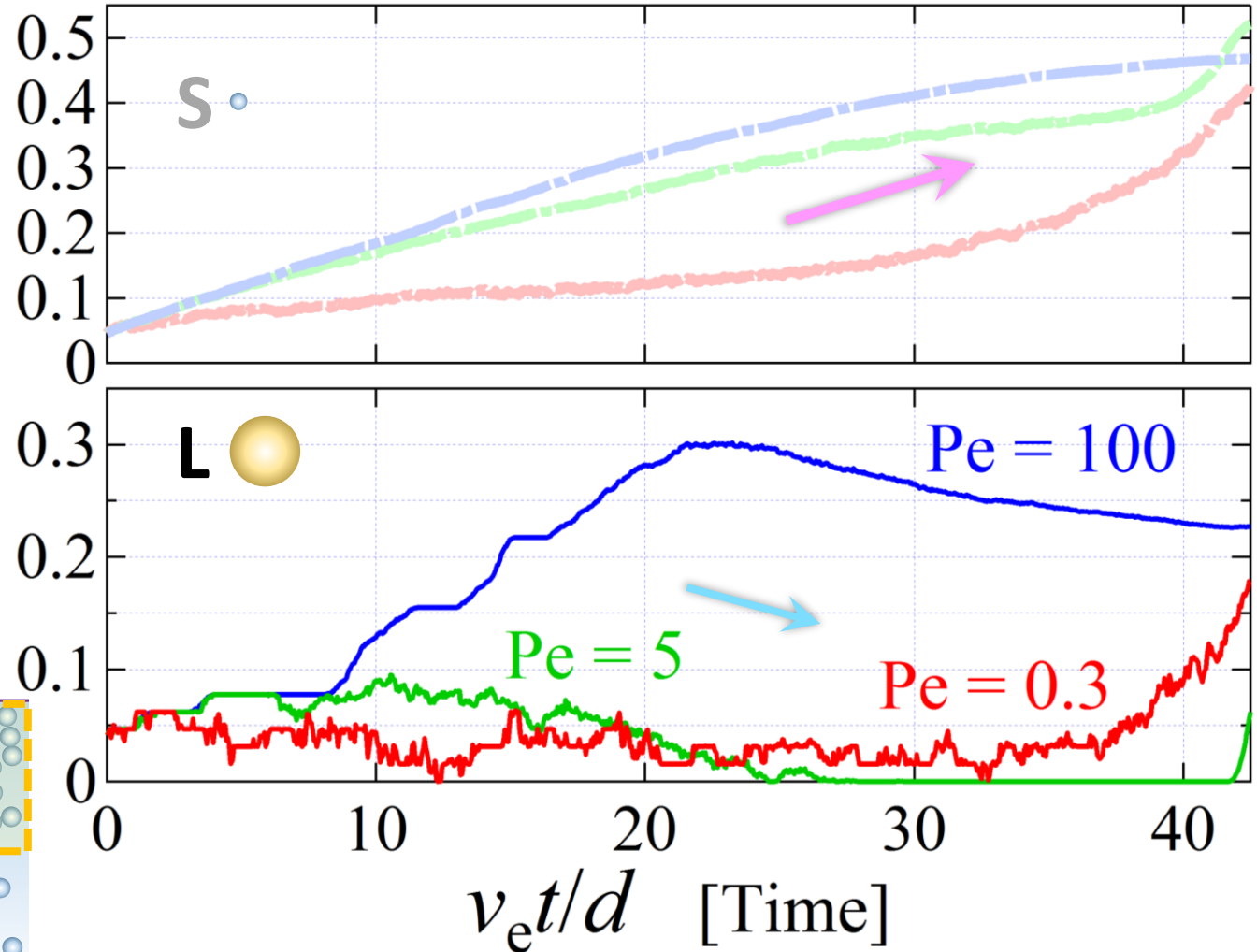
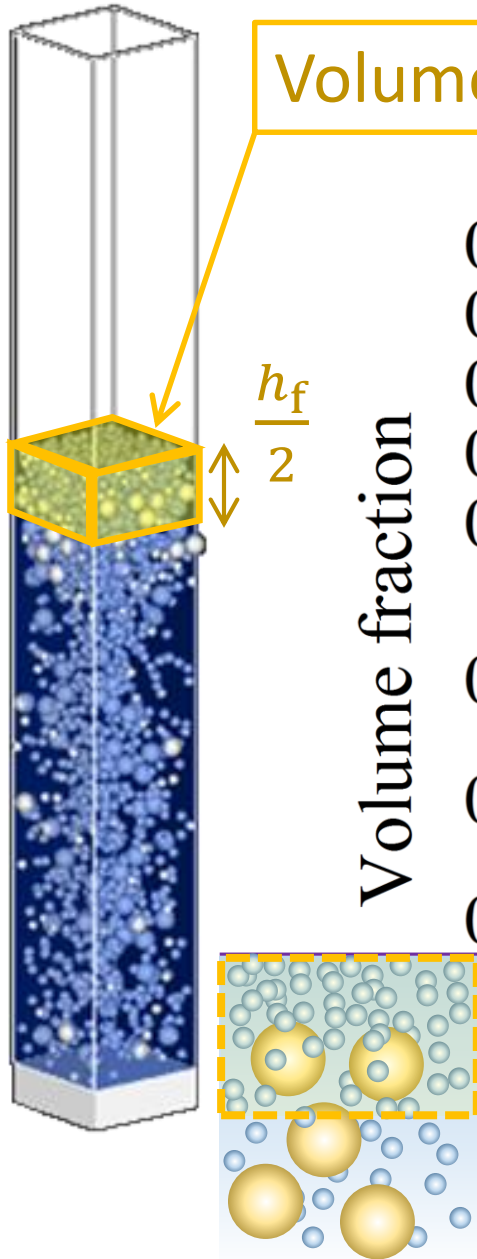
# Surface Accumulation ( $\kappa = 2$ )

Volume fraction of **L** (**S**) particles in the box



# Surface Accumulation ( $\kappa = 4$ )

Volume fraction of **L** (**S**) particles in the box

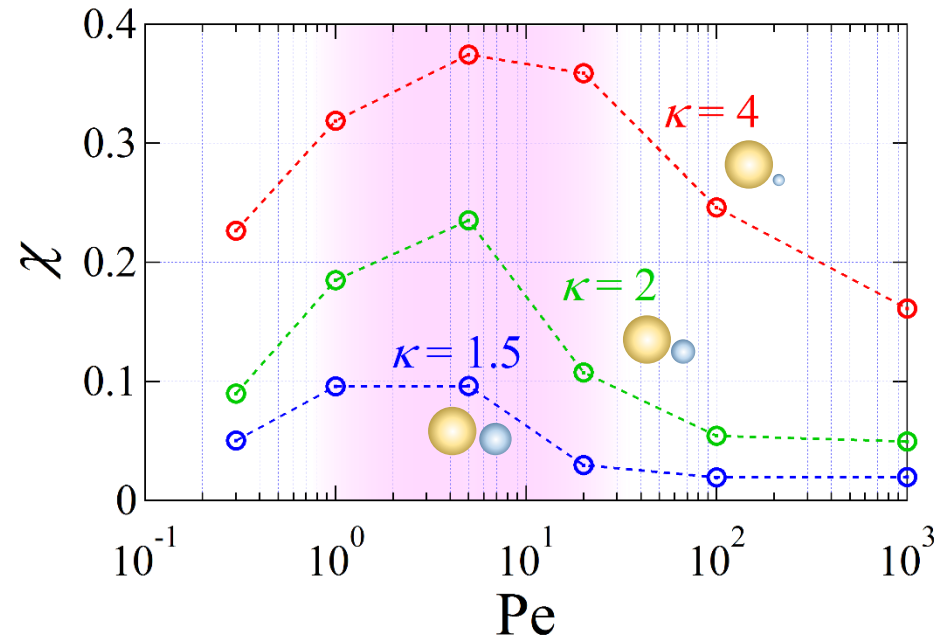




# Summary

- ◆ Segregation is reproduced by the simple model without gravity and fluid flow.

- ◆ The condition that segregation is enhanced is obtained as right figure.



- ◆ **L** particles are diffused by accumulated **S** particles. This diffusion is suppressed at low/high Péclet number.
  - Low  $Pe \rightarrow$  Less particle accumulation
  - High  $Pe \rightarrow$  Dense particle accumulation